

Rearranging in tridiagonal matrix form we get

$$\begin{array}{c}
 FC_{k-1} \qquad \qquad \qquad BC \qquad \qquad \qquad FC_k \\
 - \left[\frac{\lambda \Delta t K_{M_{k-1}}}{\Delta S^2 H_{\theta_{k-1}}^{n+1}} \right] u_{k-1}^{n+1} + \left[H_{\theta_k}^{n+1} + \frac{\lambda \Delta t K_{M_k}}{\Delta S^2 H_{\theta_k}^{n+1}} + \frac{\lambda \Delta t K_{M_{k-1}}}{\Delta S^2 H_{\theta_{k-1}}^{n+1}} \right] u_k^{n+1} - \left[\frac{\lambda \Delta t K_{M_k}}{\Delta S^2 H_{\theta_k}^{n+1}} \right] u_{k+1}^{n+1} = \\
 A \qquad \qquad \qquad B \qquad \qquad \qquad C \\
 \\
 \left[H_{\theta}^n u^n + \Delta t m n R u + \frac{\Delta t (1-\lambda)}{\Delta S^2} \left(\frac{K_{M_k}}{H_{\theta_k}^n} (u_{k+1}^n - u_k^n) - \frac{K_{M_{k-1}}}{H_{\theta_{k-1}}^n} (u_k^n - u_{k-1}^n) \right) \right] \\
 D \qquad \qquad \qquad FC_{k-1} \qquad \qquad \qquad FC_k
 \end{array}$$

Bottom ($k=1$) and top ($k=N$) values for tridiagonal coefficients A, B, C, D

$$A(1) = 0$$

$$A(2:N) = - \frac{\lambda \Delta t K_{M_{k-1}}}{\Delta S^2 H_{\theta_{k-1}}^{n+1}} \quad \& \quad \frac{\lambda \Delta t}{\Delta S^2} \frac{1}{\Delta x} = m$$

$$B(1) = H_{\theta_1}^{n+1} + \frac{\lambda \Delta t K_{M_1}}{\Delta S^2 H_{\theta_1}^{n+1}} \quad m + \& \quad \frac{\lambda \Delta t}{\Delta S^2} \frac{1}{\Delta x} = m$$

$$B(2:Nm) = H_{\theta_k}^{n+1} + \frac{\lambda \Delta t K_{M_k}}{\Delta S^2 H_{\theta_k}^{n+1}} + \frac{\lambda \Delta t K_{M_{k-1}}}{\Delta S^2 H_{\theta_{k-1}}^{n+1}} \quad : m$$

$$B(N) = H_{\theta_N}^{n+1} + \frac{\lambda \Delta t K_{M_{Nn}}}{\Delta S^2 H_{\theta_{Nn}}^{n+1}} \quad : m$$

$$C(i:Nm) = - \frac{\lambda \Delta t K_{M_k}}{\Delta S^2 H_{\theta_k}^{n+1}} \quad : m$$

$$C(N) = 0$$

$$D(1) = H_{\theta_1}^n u_1^n + \Delta t m n R u_1 + \frac{\Delta t (1-\lambda)}{\Delta S^2} \frac{K_{M_1}}{H_{\theta_1}^n} (u_2^n - u_1^n) - \frac{\Delta t}{\Delta S} \psi_b^x$$

$$D(2:Nm) = H_{\theta_k}^n u_k^n + \Delta t m n R u_k + \frac{\Delta t (1-\lambda)}{\Delta S^2} \left[\frac{K_{M_k}}{H_{\theta_k}^n} (u_{k+1}^n - u_k^n) - \frac{K_{M_{k-1}}}{H_{\theta_{k-1}}^n} (u_k^n - u_{k-1}^n) \right]$$

$$D(N) = H_{\theta_N}^n u_N^n + \Delta t m n R u_N - \frac{\Delta t (1-\lambda)}{\Delta S^2} \left[\frac{K_{M_{Nn}}}{H_{\theta_{Nn}}^n} (u_N^n - u_{Nn}^n) \right] + \frac{\Delta t}{\Delta S} \psi_s^x$$