

Tutorial 9: Normalization Factors for *Prior* Error Correlations

Prior Error Covariance Modeling

Recall: $B_x = K_b \Sigma C \Sigma^T K_b^T$

C is a correlation matrix for the unbalanced increments, and is modeled as the solution of a diffusion equation:

$$\partial \mathbf{x} / \partial t - \kappa \nabla^2 \mathbf{x} = 0 \rightarrow C' \mathbf{x}$$

But, C' is arbitrary at this stage, and must to be normalized to ensure that the range is ± 1 as required for a correlation function. Therefore we define:

$$C = \Lambda C' \Lambda^T$$

where Λ is a diagonal matrix with elements $(c_{ii}')^{-1/2}$

Finally: $B_x = K_b \Sigma \Lambda C' \Lambda^T \Sigma^T K_b^T$

Computing Λ (define NORMALIZATION)

Following Weaver & Courtier (2001) we employ two methods for computing the elements of Λ :

(i) Exact method (Nmethod=0):

$C'e_i \rightarrow i^{th}$ column of C' ; save c_{ii}

where $e_i^T = (0, 0, \dots, 0, 1, 0, \dots, 0)$
 \uparrow
 i^{th} element

Requires N_{grid} runs of diffusion operators:
impractical for v. large grids.

Computing Λ

(ii) Randomization method ($N_{method}=1$):

Estimate the diagonal elements c'_{ii} of C' from:

$$C' \approx \frac{1}{M} \sum_{i=1}^M \xi C' \xi^\top = \tilde{C}$$

where ξ is a random vector: $\xi \sim N(\mathbf{0}, \mathbf{I})$

M is the sample size. As $M \rightarrow \infty$, $\tilde{C} \rightarrow C'$
(Nrandom)

Uncertainty in elements of Λ^{-1} : $(2M)^{-1/2}$

Practical requirement: $M \ll N_{grid}$

(Fisher and Courtier, 1995)

Computing Λ

Practicalities:

- choose M and run normalization driver
- choose another seed and run again
- compare the estimates – are they similar
- compute means of the two M samples
- repeat as necessary until mean does not change significantly

Normalization Tutorial Wiki Page



WC13 C-preprocessing Options (Basic Configuration)	
Momentum Equations Options:	Model Configuration Options:
#define UV_ADV including advection terms #define VCOR including Coriolis terms #define DJ_GRADS split mass density Jacobian POF #define HOMOGENOUS harmonic horizontal mixing #define UV_VI3 harmonic c horizontal mixing #define MI_XLUV mixing along s-levels	#define SOLVE3D solve 3D primitive equations #define CURVGRID curvilinear grid #define SPHERICAL spherical grid #define PROFILE time profiling #define SPLINES parabolic splines reconstruction
Tracer Equations Options:	Lateral Boundary Conditions:
#define TS_UHADVECTION 3rd-order Upstream H. advection on #define TS_C4ADVECTION 4th-order Centered V. advection on #define TS_DI_F2 harmonic C horizontal mixing #define TS_DI_TS harmonic T horizontal mixing #define SALINITY including salt in ty #define SALT_LCOS non linear equation of state #define AML_STFLUX analytical bottom Temp Flux #define AML_ISFLUX analytical bottom Salt Flux	#define EASTERN_WALL closed eastern wall condition #define WEST_FISCHMAN free-surface, Chapman #define WEST_ISPLATHER 2D momentum, Flather #define WEST_ISCLAMPED 3D momentum, clamped #define WEST_TCCLAMPED tracers, clamped condition
Vertical Turbulent Mixing Parameterization:	#define NORTH_FISCHMAN free-surface, Chapman #define NORTH_ISPLATHER 2D momentum, Flather #define NORTH_ISCLAMPED 3D momentum, clamped #define SOUTH_FISCHMAN free-surface, Chapman #define SOUTH_ISPLATHER 2D momentum, Flather #define SOUTH_ISCLAMPED 3D momentum, clamped #define SPONGE enhanced viscous/tdiffusion areas
#define GLS_MIXING Generic Length Scale Mixing #if !defined GLS_MIXING #define KSSZ_HOBINS smoothing of buoyancy/shear #define KANTHA_CLAYSON stability function #endif #define ATMOSPHERIC_BOUNDARY_LAYER_PARAMETERIZATION: #define BULK_FLUXES Air/sea COAG bulk fluxes #define DIURNAL_SFLLUX imposing local diurnal cycle #define SOLAR_SOURCE solar radiation source term #define SOLAR_SOURCE_OUT compute outgoing long wave rad #define EMISSP compute E-p	

WC13 C-preprocessing Options (Error Covariance Normalization)	
Algorithm:	
#define Normalization compute 4D-Var error covariance normalization coefficients	
Control Vector:	
#define ADJUST_BOUNDARY open boundary conditions increments #define ADJUST_SFLLUX surface tracer flux increments #define ADJUST_WSTRESS surface wind stress increments	
Error Covariance Modeling:	
#define CORRELATION model error covariance correlation with diffusion operators #define FULL_GRID consider both interior and boundary points #define VCONVOLUTION Vertical correlation modeling #define IMPLICIT_VCON Implicit vertical diffusion operator #define BALANCE_OPERATOR Multivariate balance constraint #define BALANCE_OPERATOR #define ZETA_ELLIPTIC SSH elliptic equation method #endif	
Prior:	
#define FORWARD_READ read basic state linearization in TLM and ADM files #define FORWARD_WRI read basic state by the NLM #define FORWARD_MIXING processing basic state vertical mixing coefficients #define NL_BULK_FLUXES surface kinematic fluxes from nonlinear model	
I/O:	
#define OUT_DOUBLE double precision data in output NLM, TLM, RPM, and ADM	

WC13 C-preprocessing Options (Error Covariance Normalization)	
Algorithm:	
#define Normalization compute 4D-Var error covariance normalization coefficients	
Control Vector:	
#define ADJUST_BOUNDARY open boundary conditions increments #define ADJUST_SFLLUX surface tracer flux increments #define ADJUST_WSTRESS surface wind stress increments	
Error Covariance Modeling:	
#define CORRELATION model error covariance correlation with diffusion operators #define FULL_GRID consider both interior and boundary points #define VCONVOLUTION Vertical correlation modeling #define IMPLICIT_VCON Implicit vertical diffusion operator #define BALANCE_OPERATOR Multivariate balance constraint #define BALANCE_OPERATOR #define ZETA_ELLIPTIC SSH elliptic equation method #endif	
Prior:	
#define FORWARD_READ read basic state linearization in TLM and ADM files #define FORWARD_WRI read basic state by the NLM #define FORWARD_MIXING processing basic state vertical mixing coefficients #define NL_BULK_FLUXES surface kinematic fluxes from nonlinear model	
I/O:	
#define OUT_DOUBLE double precision data in output NLM, TLM, RPM, and ADM	

Include File: wc13.h

```
/*
 * gnu f90 wlcl13.f90 476 2010-06-26 20:25:30Z armmp $ 
*****
 * Copyright (c) 2002-2010 The ROMS/TOMS Group
 * Licensed under a MIT/X style license
 * See License_ROMS.txt
***** 

** Options for the California Current System, 1/3 degree resolution.
** Application flag: WLCL3
** Input script: ocean_wlcl3.in
**                         sdvar.in

Available Drivers options: choose only one and activate it in the
build.sh script (MY_CPP_FLAGS definition)

** ADD SENSITIVITY          Additive sensitivity Driver
** AFT EIGENMODES            Adjoint Finite Time Eigendmodes
** ARRAY MODES               Stabilized representer matrix array modes
** CLIPPING                  Stabilized representer matrix clipped analysis
** GRADIENT CHECK            Gradient Check
** GRADIENT CHECK 4DVAR      TLM/ADM Gradient Check
** FORCING SV                Forcing Singular Vectors
** FT EIGENNODES              Finite Time Eigennodes
** IS4DVAR                   Incremental State constraint 4DVAR
** LSQ PREDICTION             Nonlinear Least State trajectory
** OPT. PERTURBATION          Optimal perturbations
** PICARD TEST                Picard Iterations Test
** R-SYMMETRY                 Represented Matrix Symmetry Test
** R-SYMMETRY CHECK            Statis Check
** SO SEMI                   Stochastic Optimal: Semi-norm
```

4D-Var Error Covariance Normalization Files

- Four different error covariance normalization coefficients NetCDF files are required in ROMS 4D-Var algorithms to ensure that the diagonal elements of the associated correlation matrix (**C**) are equal to unity:
 - Model error normalization file, if weak constraint
 - Initial conditions normalization file
 - Open boundary conditions normalization file, if **ADJUST_BOUNDARY**
 - Surface forcing normalization file, if **ADJUST_WSTRESS** and/or **ADJUST_STFLUX**
 - These normalization NetCDF files are specified in 4D-Var input script as:

```
NRMnameM == ./Data/wc13_nrm_m.nc  
NRMnameI == ./Data/wc13_nrm_I.nc  
NRMnameB == ./Data/wc13_nrm_b.nc  
NRMnameF == ./Data/wc13_nrm_f.nc
```

Model Error and Initial Conditions Metadata

Open Boundary Conditions Metadata

Surface Forcing Metadata

Standard Input File: ocean_wc13.in

```

ROMS/TOMS Standard Input parameters.

$vn $id: ocean_wcl3.in 476 2010-06-26 20:25:30Z arango 6
$Copyright (c) 2002-2010 The ROMS/TOMS Group
$Licensed under a MIT/X style license
$See License_ROMS.txt

1. Parameters can be entered in ANY order, provided that the parameter KEYWORD (usually a variable name) is typed correctly followed by "=" and "=". All comment lines are allowed and must begin with an exclamation mark (!) in column one. Comments may appear to the right of a parameter value. Continuation lines are allowed and must be preceded by a backslash (\). Blank lines are also allowed and ignored. Continuation lines in a parameter specification are allowed and must be preceded by a backslash (\). In some instances, more than one value is required for a parameter. A few parameters are preceded by a colon (:) as shown below the parameter array entry. The multiplication symbol (*), without blank spaces in between, is allowed for a parameter specification. For example, in a two grids nested application:

  AKT_BAK == 2*0.6-6 2*0.6-6                                ! m/s

indicates that the first two entries of array AKT_BAK, in Fortran column-major order, will have the same value of *1.04*-6 for grid 1, whereas the next two entries will have the same value of *5.04*-6 for grid 2.

In multiple levels of nesting and/or multiple connected domains step-ups, "Ngrids" entries are expected for some of these parameters. In such case, the order of the entries for a parameter is extremely important. It must

```

c4dvar.in Important Parameters

```

Nmethod == 0           ! normalization method (0: exact, 1:randomization)
Nrandom == 5000        ! randomization iterations

LdefNRM == T T T T     ! Create a new normalization files
LwrNRM == T T T T     ! Compute and write normalization
.

CnormI(isFsur) == T   ! 2D variable at RHO-points
CnormI(isUbar) == T   ! 2D variable at U-points
CnormI(isVbar) == T   ! 2D variable at V-points
CnormI(isUvel) == T   ! 3D variable at U-points
CnormI(isVvel) == T   ! 3D variable at V-points
CnormI(isTvar) == T   ! NT tracers
.

CnormB(isFsur) == T   ! 2D variable at RHO-points
CnormB(isUbar) == T   ! 2D variable at U-points
CnormB(isVbar) == T   ! 2D variable at V-points
CnormB(isUvel) == T   ! 3D variable at U-points
CnormB(isVvel) == T   ! 3D variable at V-points
CnormB(isTvar) == T   ! NT tracers
.

CnormF(isUstr) == T   ! surface U-momentum stress
CnormF(isVstr) == T   ! surface V-momentum stress
CnormF(isTsur) == T   ! NT surface tracers flux
.

NRMnameE == wc13_nrm_m.nc ! model error (weak constraint)
NRMnameI == wc13_nrm_i.nc ! initial conditions
NRMnameB == wc13_nrm_b.nc ! open boundary conditions
NRMnameF == wc13_nrm_f.nc ! surface forcing (wind stress and net heat flux)

```

Normalization Method

- The **exact method** is very expensive on large grids.
- The normalization coefficients are computed by perturbing each model grid cell with a delta function scaled by the area (2D state variables) or volume (3D state variables), and then convolving with the squared-root adjoint and tangent linear diffusion operators.
- The **randomization method** is cheaper (Fisher and Courtier, 1985).
- The normalization coefficients are initialized with random numbers having a uniform distribution (drawn from a normal distribution with zero mean and unit variance). Then, they are scaled by the inverse squared-root of the cell area (2D state variables) or volume (3D state variables) and convolved with the squared-root adjoint and tangent linear diffusion operator over a specified number of iterations, **Nrandom**.
- The normalization coefficients need to be computed only once for a particular application provided that the grid, land/sea masking (if any), and decorrelation scales remain the same.

4D-Var Parameters: Decorrelation Scales

```

Horizontal and vertical stability and accuracy factors (< 1):

!          IC      Model      OBC      Sur For
Hgamma = 0.5    0.5    0.5    0.5    ! horizontal operator
Vgamma = 0.0005  0.0005  0.0005  0.0005 ! vertical operator

Model_Error correlations (m):

HdecayM(isFsur) == 50.0d+3           ! free-surface
HdecayM(isUbar) == 50.0d+3           ! 2D U-momentum
HdecayM(isVbar) == 50.0d+3           ! 2D V-momentum
HdecayM(isUvel) == 50.0d+3           ! 3D U-momentum
HdecayM(isVvel) == 50.0d+3           ! 3D V-momentum
HdecayM(isTvar) == 50.0d+3           ! 1:NT tracers

VdecayM(isUvel) == 30.0d0             ! 3D U-momentum
VdecayM(isVvel) == 30.0d0             ! 3D V-momentum
VdecayM(isTvar) == 30.0d0             ! 1:NT tracers

```

4D-Var Parameters: Decorrelation Scales

```
Initial conditions correlations (m):
HdecayI(isFsur) == 50.0d+3          ! free-surface
HdecayI(isUbar) == 50.0d+3          ! 2D U-momentum
HdecayI(isVbar) == 50.0d+3          ! 2D V-momentum
HdecayI(isUvel) == 50.0d+3          ! 3D U-momentum
HdecayI(isVvel) == 50.0d+3          ! 3D V-momentum
HdecayI(isTvar) == 50.0d+3          ! 1:NT tracers

VdecayI(isUvel) == 30.0d0           ! 3D U-momentum
VdecayI(isVvel) == 30.0d0           ! 3D V-momentum
VdecayI(isTvar) == 30.0d0 30.0d0    ! 1:NT tracers

Surface forcing correlations (m):
HdecayF(isUstr) == 100.0d+3         ! surface U-momentum stress
HdecayF(isVstr) == 100.0d+3         ! surface V-momentum stress
HdecayF(isTsur) == 100.0d+3 100.0d+3 ! 1:NT surface tracer flux
```

4D-Var Parameters: Decorrelation Scales

```
Open boundary conditions correlations (m):
!
! 1: west 2: south 3: east 4: north
HdecayB(isFsur) == 100.0d+3 100.0d+3 100.0d+3 100.0d+3 ! free-surface
HdecayB(isUbar) == 100.0d+3 100.0d+3 100.0d+3 100.0d+3 ! 2D U-momentum
HdecayB(isVbar) == 100.0d+3 100.0d+3 100.0d+3 100.0d+3 ! 2D V-momentum
HdecayB(isUvel) == 100.0d+3 100.0d+3 100.0d+3 100.0d+3 ! 3D U-momentum
HdecayB(isVvel) == 100.0d+3 100.0d+3 100.0d+3 100.0d+3 ! 3D V-momentum
HdecayB(isTvar) == 4*100.0d+3 4*100.0d+3 ! 1:NT tracers

VdecayB(isUvel) == 30.0d0 30.0d0 30.0d0 30.0d0 ! 3D U-momentum
VdecayB(isVvel) == 30.0d0 30.0d0 30.0d0 30.0d0 ! 3D V-momentum
VdecayB(isTvar) == 4*30.0d 4*30.0d ! 1:NT tracers

Boundary edges to adjust (logical switches):
!
!      1   2   3   4
!      |   |   |   |
!      North
Lobc(isFsur) == T T F T ! free-surface
Lobc(isUbar) == T T F T ! 2D U-momentum
Lobc(isVbar) == T T F T ! 2D V-momentum
Lobc(isUvel) == T T F T ! 3D U-momentum
Lobc(isVvel) == T T F T ! 3D V-momentum
Lobc(isTvar) == T T F T ! 1:NT tracers
!
!      1   2   3   4
!      |   |   |   |
!      West
Lobc(isFsur) == T T F T ! free-surface
Lobc(isUbar) == T T F T ! 2D U-momentum
Lobc(isVbar) == T T F T ! 2D V-momentum
Lobc(isUvel) == T T F T ! 3D U-momentum
Lobc(isVvel) == T T F T ! 3D V-momentum
Lobc(isTvar) == T T F T ! 1:NT tracers
!
!      1   2   3   4
!      |   |   |   |
!      East
Lobc(isFsur) == T T F T ! free-surface
Lobc(isUbar) == T T F T ! 2D U-momentum
Lobc(isVbar) == T T F T ! 2D V-momentum
Lobc(isUvel) == T T F T ! 3D U-momentum
Lobc(isVvel) == T T F T ! 3D V-momentum
Lobc(isTvar) == T T F T ! 1:NT tracers
!
!      1   2   3   4
!      |   |   |   |
!      South
Lobc(isFsur) == T T F T ! free-surface
Lobc(isUbar) == T T F T ! 2D U-momentum
Lobc(isVbar) == T T F T ! 2D V-momentum
Lobc(isUvel) == T T F T ! 3D U-momentum
Lobc(isVvel) == T T F T ! 3D V-momentum
Lobc(isTvar) == T T F T ! 1:NT tracers
```

Normalization Parameters File: c4dvar.in

```
! 4DVar assimilation input parameters.
! evn fidi: s4dvar.in 1256 2010-06-12 21:59:26 grango $
=====
!===== Copyright (c) 2002-2010 The ROMS/TOMS Group =====
!===== Licensed under a MIT/X style license =====
!===== See License_ROMS.txt =====
=====
!
! Input parameters can be entered in ANY order, provided that the parameter
! name is uniquely, upper case, it is typed correctly followed by "=" or "*="
! symbol. Any comment lines are allowed and must begin with an exclamation
! mark (!) in column one. Comments may appear to the right of a parameter
! specification to improve documentation. Comments will be ignored during
! reading. Blank lines are also allowed and ignored. Continuation lines in
! parameter specifications are allowed and must be preceded by a backslash
! (\). In some instances, more than one value is required for a parameter.
! If fewer values are provided, the last value is assigned for the entire
! parameter array. The multiplication symbol (*), without blank spaces in
! between is allowed for a parameter specification. For example, in a two
! grids nested application:
!
!     ARK_BAK == 2*1.0d-6 2*5.0d-6 ! m2/s
!
! indicates that the first two entries of array ARK_BAK, in fortran column-
! major order, will have the same value of "1.0d-6" for grid 1, whereas the
! next two entries will have the same value of "5.0d-6" for grid 2.
!
! In multiple levels of nesting and/or multiple connected domains step-ups,
! "Ngrids" entries are expected for some of these parameters. In such case,
! the order of the entries for a parameter is extremely important. It must
! follow the same order (1:Ngrids) as in the state variable declaration. The !
```

Job Script: job_normalization.sh

```

1. Set path definition to one directory up in the tree.      6. Modify 4D-Var template input script and specify
   set Dir = `dirname $PWD`                                above files.

2. Set string manipulations perl script.                    set Norm = cdvar.in
   set SUBSTITUTE = ${HOME}_ROOT/RMWS/BIN/subst1.tute
   cp -p ${Dir}/Data/wc13_in.nc wc13_in.nc
   cp ${Dir}/Data/wc13_in.nc ${Norm}
   set SUBSTITUTE = ${HOME}_ROOT/RMWS/BIN/subst1.tute
   cp ${Norm} ${Dir}/cdvar.in
   SUBSTITUTE SNORM ocean_std_u.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_b.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_v.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_w.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_u.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_b.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_v.nc SSTdaniel
   SUBSTITUTE SNORM ocean_std_w.nc SSTdaniel
   SUBSTITUTE SNORM ocean_pbs.nc wc13_pbs.nc
   SUBSTITUTE SNORM ocean_pbc.nc wc13_pbc.nc
   SUBSTITUTE SNORM ocean_pbw.nc wc13_pbw.nc
   SUBSTITUTE SNORM ocean_pbd.nc wc13_pbd.nc
   SUBSTITUTE SNORM ocean_err.nc wc13_err.nc
   set STDnameA = ./Data/wc13_std_u.nc
   set STDnameB = ./Data/wc13_std_b.nc
   set STDnameC = ./Data/wc13_std_v.nc
   set STDnameD = ./Data/wc13_std_w.nc
   set STDnameE = ./Data/wc13_std_pbs.nc
   set STDnameF = ./Data/wc13_std_pbc.nc
   set STDnameG = ./Data/wc13_std_pbw.nc
   set STDnameH = ./Data/wc13_std_pbd.nc
   set STDnameI = ./Data/wc13_std_err.nc

```

Job Script File: job_normalization.sh

```

#!/bin/csh -f
# svr $Id: job_normalization.sh 474 2010-06-25 20:19:44Z arango $
#####
# Copyright (c) 2009-2010 The ROMS/TOMS Group
# Licensed under a MIT/X style license
# See License_ROMS.txt
#####
# 4D-Var error covariance normalization coefficients job script:
#
# This script NEEDS to be run before any run:
#
# (1) It copies a new clean nonlinear model initial conditions
#     file. The nonlinear model is initialized from the
#     background or reference state.
# (2) Supply model, initial conditions, boundary conditions, and
#     surface forcing error covariance input standard deviations
#     files.
# (3) Supply model, initial conditions, boundary conditions, and
#     surface forcing error covariance input/output normalization
#     factor filenames.
# (4) Create 4D-Var input script "cdvar.in" from a template and
#     specify the error covariance standard deviation, and error
#     covariance normalization factors files to be used.
#
#####
# Set path definition to one directory up in the tree.
set Dir=`dirname $PWD`:

```

Compile: build.sh

```

1. Set a local environmental variable to define the path to the
   directory where all this project's files are kept.
   setenv MY_ROOT_DIR /home/arango/ocesn/toms/repository
   setenv MY_PROJECT_DIR ${PWD}

2. Location of your ROMS source code.
   setenv MY_ROMS_SRC ${MY_ROOT_DIR}/branches/arango

3. Build script invoked CPP options.
   setenv MY_CPP_FLAGS "-DNORMALIZATION"

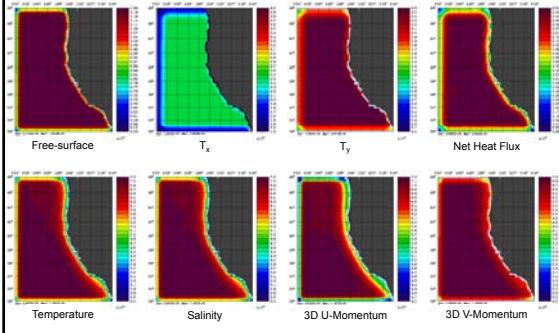
4. Compiler selection environment variables.
   setenv USE_MPI on
   setenv USE_PGI on
   setenv FORT pgi
   Libraries for PGI
   if ($USE_MPI) then
     switch ($FORT)
       case "pgi"
         setenv ARPACK_LIBDIR /opt/pgi soft/serial/ARPACK
       end
       if ($USE_MPI) then
         setenv PARPACK_LIBDIR /opt/pgi soft/api/ch/PARPACK
       end
     end
   end
   if ($USE_MPI) then
     if ($TRUE_MPI) then
       setenv NETCDF_INCDIR /opt/pgi soft/api/ch/netcdf4/include
       setenv NETCDF_LIBDIR /opt/pgi soft/api/ch/netcdf4/lib
       setenv HDF5_LIBDIR /opt/pgi soft/api/ch/hdf5/lib
     else
       setenv NETCDF_INCDIR /opt/pgi soft/serial/netcdf4/include
       setenv NETCDF_LIBDIR /opt/pgi soft/serial/netcdf4/lib
       setenv HDF5_LIBDIR /opt/pgi soft/serial/hdf5/lib
     end
   else
     setenv NETCDF_INCDIR /opt/pgi soft/api/ch/netcdf3/include
     setenv NETCDF_LIBDIR /opt/pgi soft/api/ch/netcdf3/lib
   end
   breaksw

```

Build Script: build.sh

```
#!/bin/csh -f
# $Id: build.sh 474 2010-06-25 20:19:44Z arango $
# Copyright (c) 2002-2010 The ROMS/TOMS Group
# Licensed under a MIT/X style license
# See License_ROMS.txt
# $Id: build.sh 474 2010-06-25 20:19:44Z arango $
#
# ROMS/TOMS Compiling Script
#
# Script to compile an user application where the application-specific
# files are kept separate from the ROMS source code.
#
# Q: How/Why does this script work?
#
# A: The ROMS makefile configures user-defined options with a set of
# flags such as ROMS_APPLICATION. Broader makefiles typically use
# local options in the application-specific makefile to override the
# default, this means that make will check whether an environment
# variable by that name is set in the shell that calls make. If so
# the environment variable value overrides the default (and the
# user need not maintain separate makefiles, or frequently edit
# the makefile, to run separate applications).
#
# Usage:
#   ./build.sh [options]
#
# Options:
#   -j [N]      Compile in parallel using N CPUs
```

Error Covariance Normalization Coefficients



References

- Fisher, M. and P. Courtier, 1995: Estimating the covariance matrices of analysis and forecast error in variational data assimilation. ECMWF Tech. Memo, **220**.
- Weaver, A.T. and P. Courtier, 2001: Correlation modelling on the sphere using a generalized diffusion equation. *Q. J. R. Meteorol. Soc.*, **127**, 1815-1846.